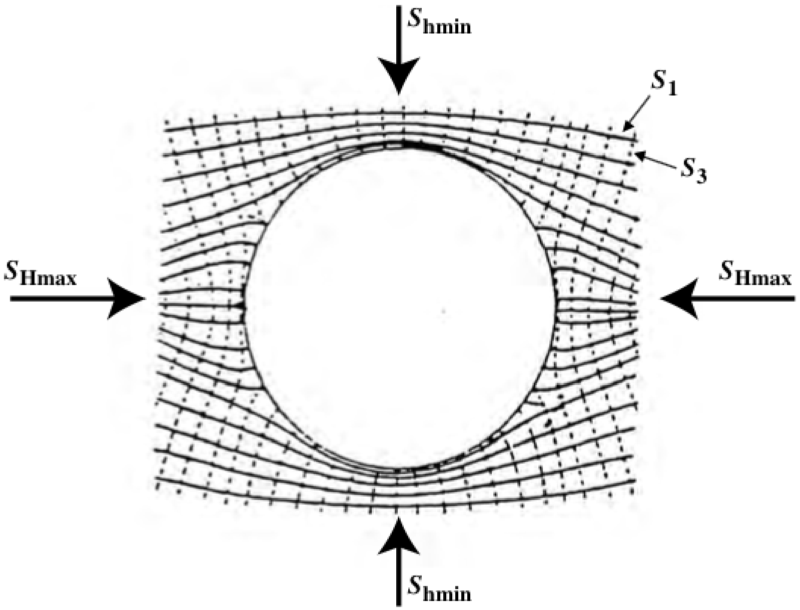
Compressive and tensile failure in vertical wells

Stress around circular cavity



 Zoback, *Reservoir Geomechanics* (Fig. 6.1, pp. 169)

Kirsch solution

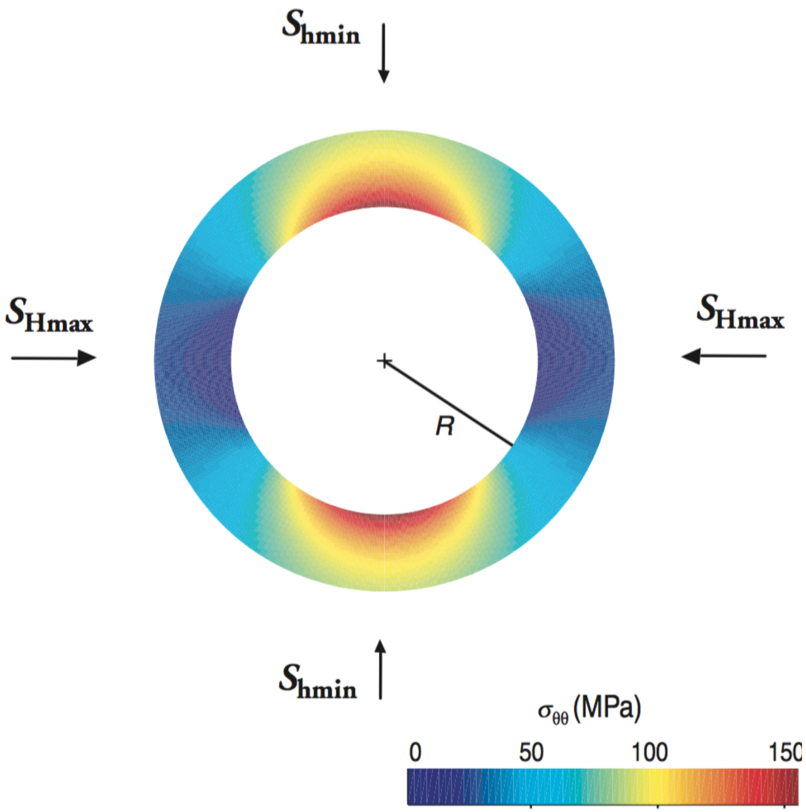
$$\sigma_{rr} = \frac{\sigma_{Hmax} + \sigma_{hmin}}{2}\left(1 - \frac{a^2}{r^2}\right) + \frac{\sigma_{Hmax} - \sigma_{hmin}}{2}\left(1 - 4\frac{a^2}{r^2} + 3\frac{a^4}{r^4}\right)\cos 2\theta + (P_w - P_p)\left(\frac{a^2}{r^2}\right)$$

$$\sigma_{\theta\theta} = \frac{\sigma_{Hmax} + \sigma_{hmin}}{2}\left(1 + \frac{a^2}{r^2}\right) - \frac{\sigma_{Hmax} - \sigma_{hmin}}{2}\left(1 + 3\frac{a^4}{r^4}\right)\cos 2\theta - (P_w - P_p)\left(\frac{a^2}{r^2}\right)$$

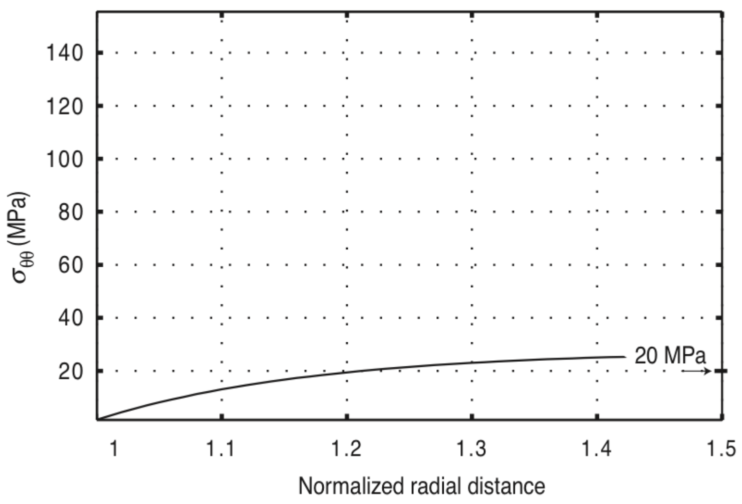
$$\sigma_{r\theta} = \frac{\sigma_{Hmax} - \sigma_{hmin}}{2}\left(1 + 2\frac{a^2}{r^2} - 3\frac{a^4}{r^4}\right) - \sin 2\theta$$

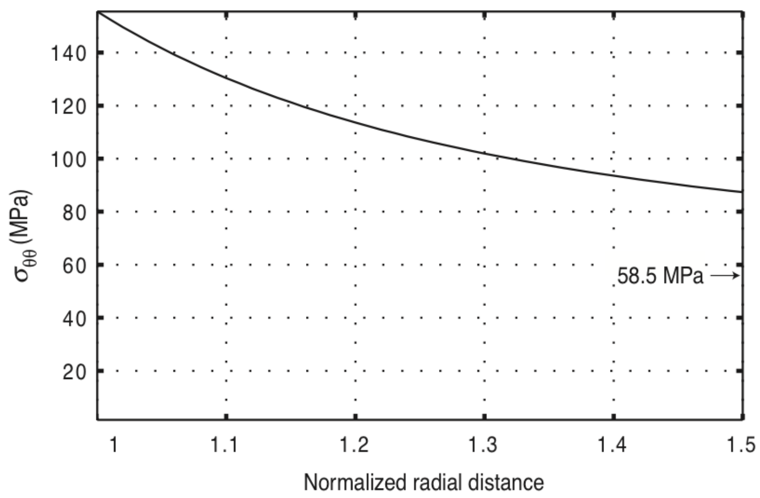
$$\sigma_{zz} = \sigma_v - 2\nu(\sigma_{Hmax} - \sigma_{hmin})\left(\frac{a^2}{r^2}\right)\cos 2\theta$$

Example



$$S_{Hmax} = 90\text{MPa}$$
$$S_v = 88.2\text{MPa}$$
$$S_{hmin} = 51.5\text{MPa}$$
$$P_p = 31.5\text{MPa}$$
$$P_w = 31.5\text{MPa}$$



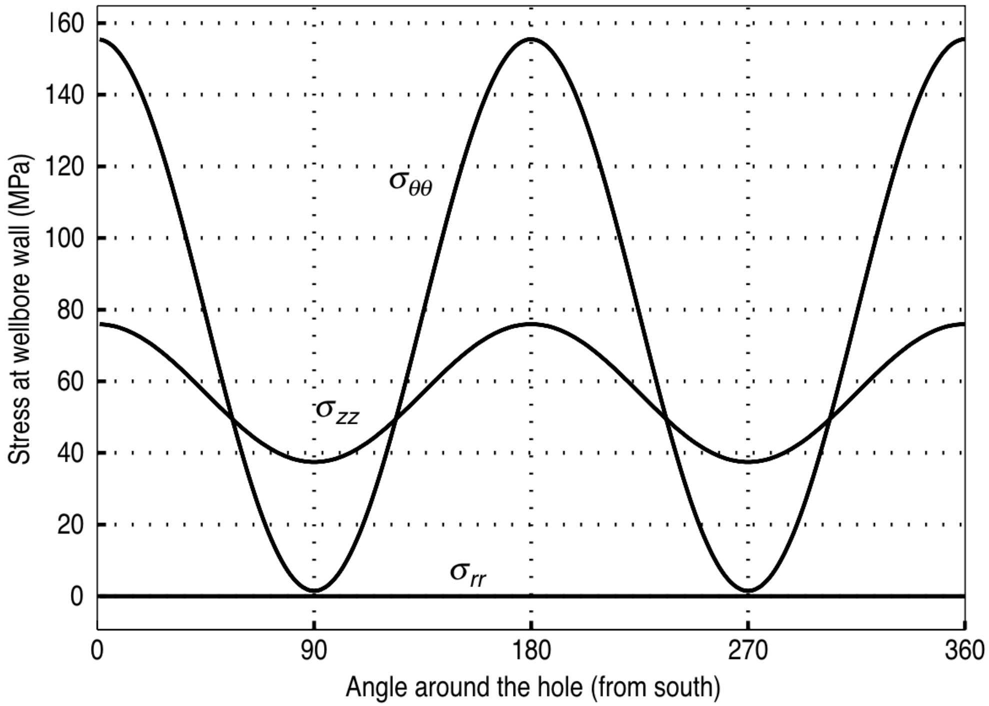


Along azimuth of S_{Hmax}

Along azimuth of S_{hmin}

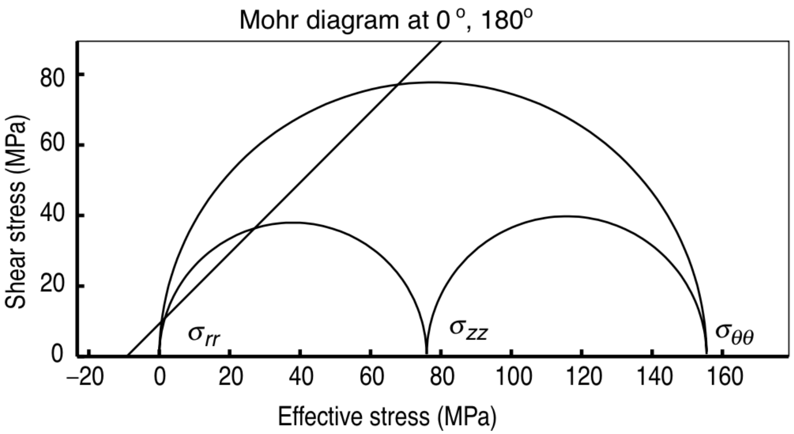
TEXAS
The University of Texas at Austin

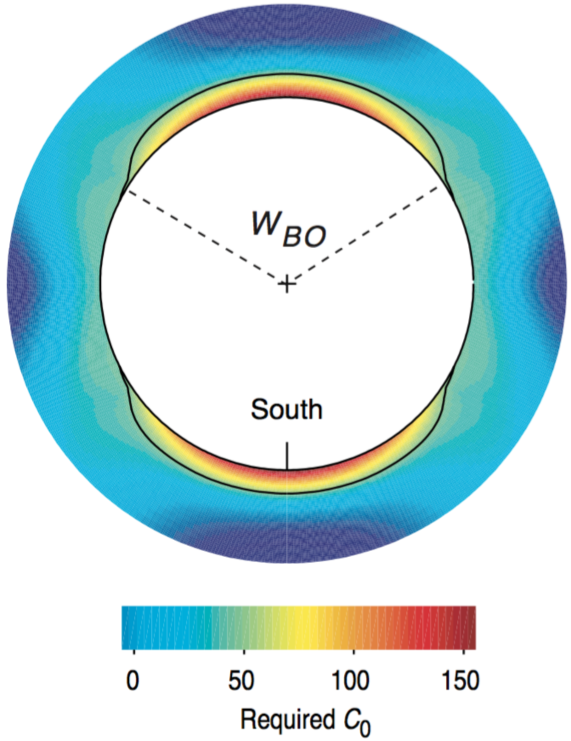
Variation of wellbore stresses



 Zoback, *Reservoir Geomechanics* (Fig. 6.3a, pp. 173)

Wellbore breakout region

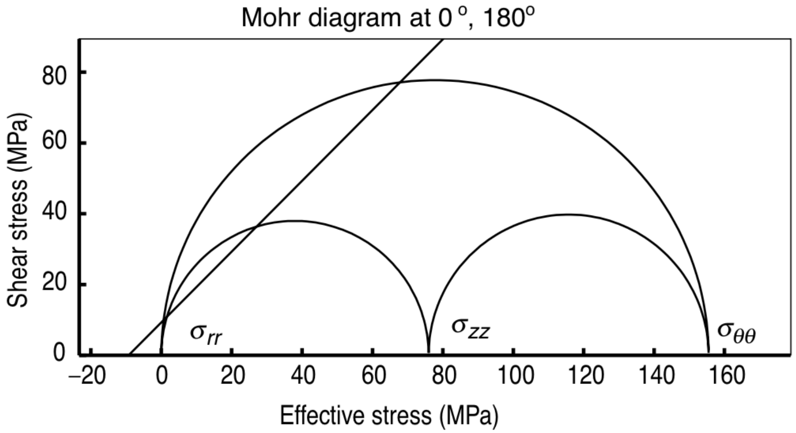


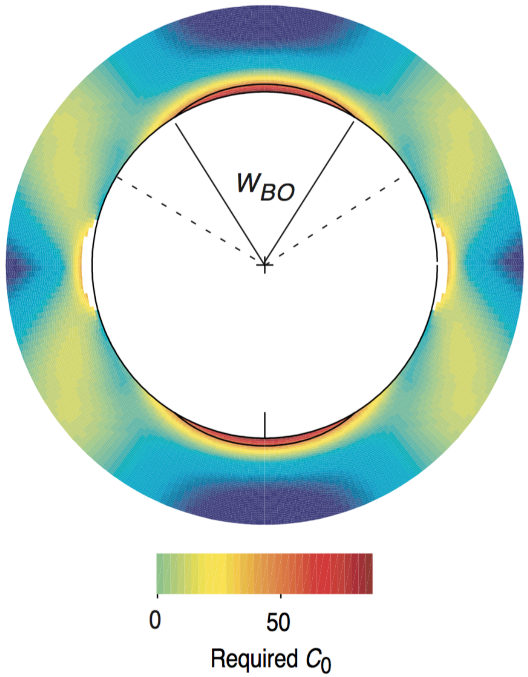


 Zoback, *Reservoir Geomechanics* (Fig. 6.3b,c, pp. 173)

Mudweight stabilization

As ΔP increases, $\sigma_{\theta\theta}$ decreases and σ_{rr} increases.





 Zoback, *Reservoir Geomechanics* (Fig. 6.3b, pp. 173 and Fig. 6.5a, pp. 177)

Breakouts as indicators of far-field stresses

Simplify Kirsch equations at wellbore wall $a = r$, so

$$\begin{aligned}\sigma_{rr} &= (P_w - P_p) = \Delta P \\ \sigma_{\theta\theta} &= \sigma_{Hmax} + \sigma_{hmin} - 2(\sigma_{Hmax} - \sigma_{hmin}) \cos 2\theta - \Delta P \\ \sigma_{zz} &= \sigma_v - 2\nu(\sigma_{Hmax} - \sigma_{hmin}) \cos 2\theta\end{aligned}$$

$\sigma_{\theta\theta}$ has min at 0° and 180°

$$\sigma_{\theta\theta}^{min} = 3\sigma_{Hmin} - \sigma_{Hmax} - \Delta P$$

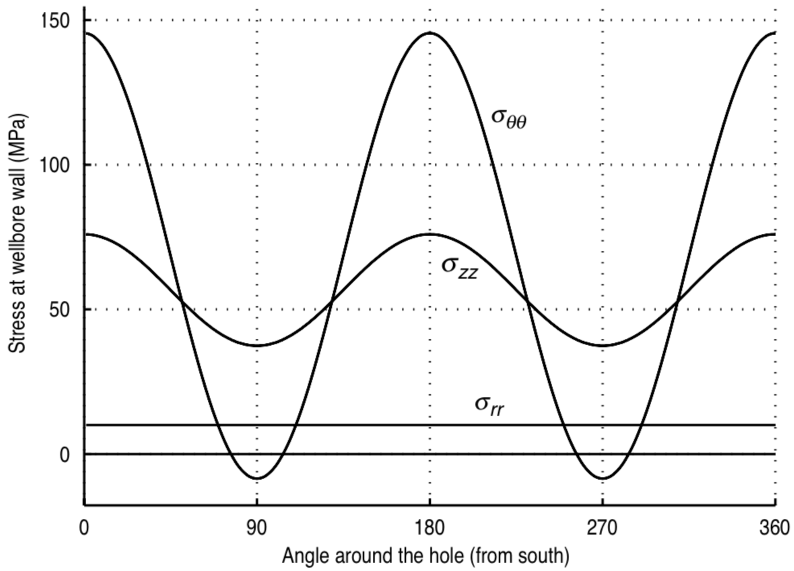
$\sigma_{\theta\theta}$ has min at 90° and 270°, so

$$\sigma_{\theta\theta}^{max} = 3\sigma_{Hmax} - \sigma_{hmin} - \Delta P$$

so

$$\sigma_{\theta\theta}^{max} - \sigma_{\theta\theta}^{min} = 4(\sigma_{Hmax} - \sigma_{hmin})$$

Tensile induced fractures

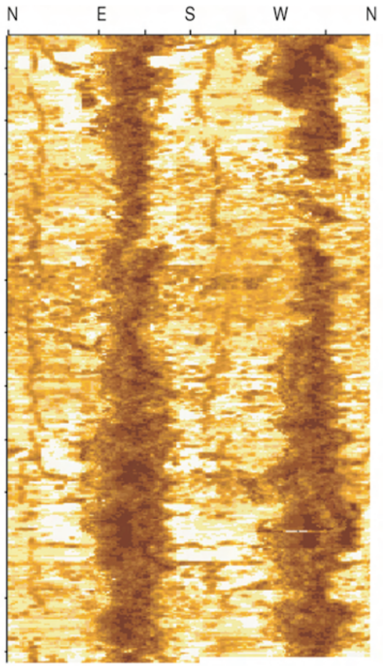


© Cambridge University Press Zoback, *Reservoir Geomechanics* (Fig. 6.5a, pp. 177)

Safe drilling mud window

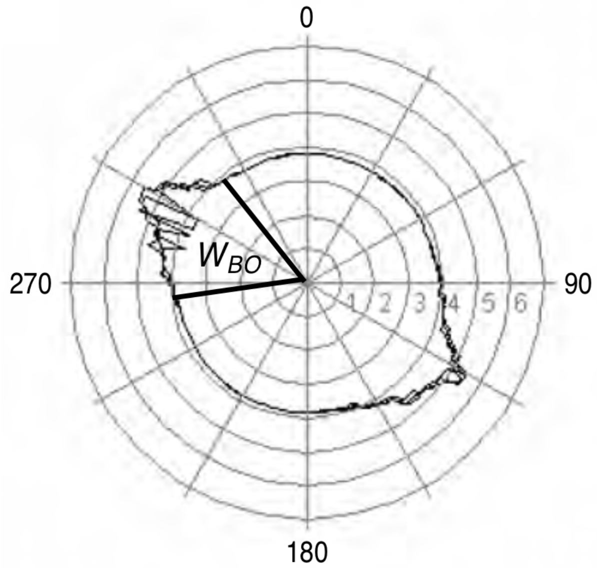
- **Mud weight too low**
  - Breakouts
- **Mud weight too high**
  - Tensile induced fractures leading to lost circulation

Imaging breakouts



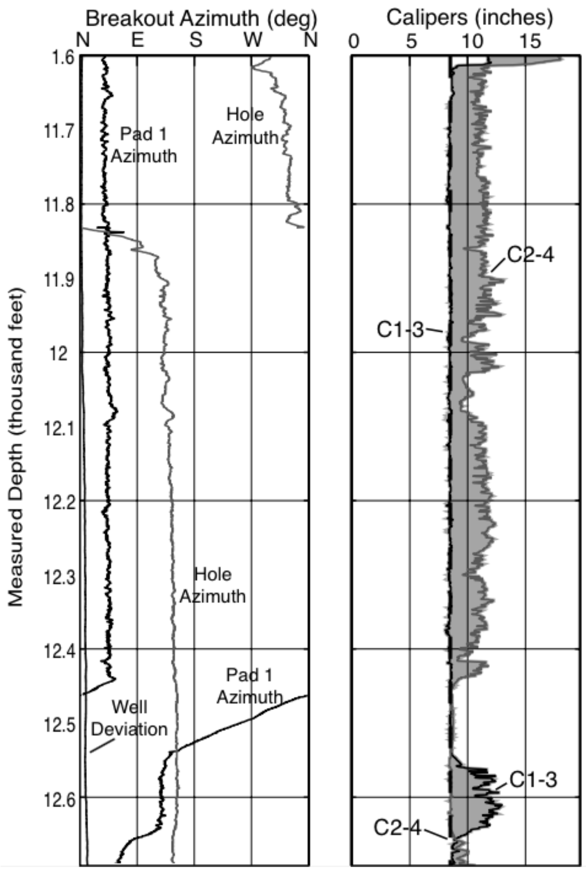
Ultrasonic *P*-wave

Electrical resistivity

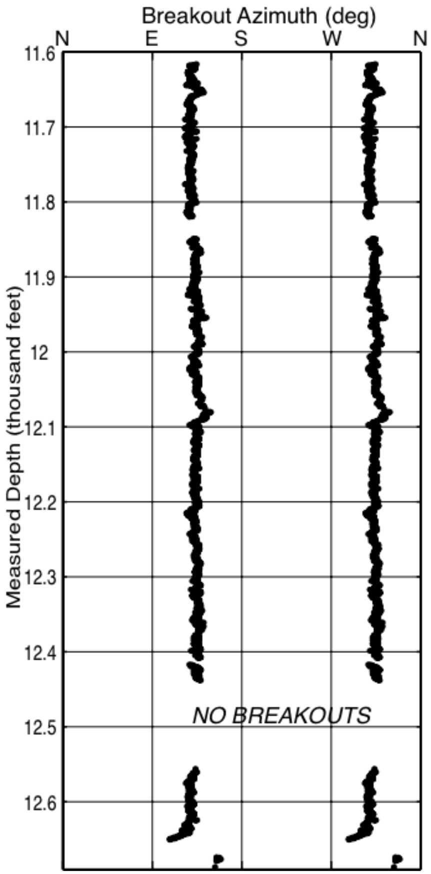


Breakout cross-section

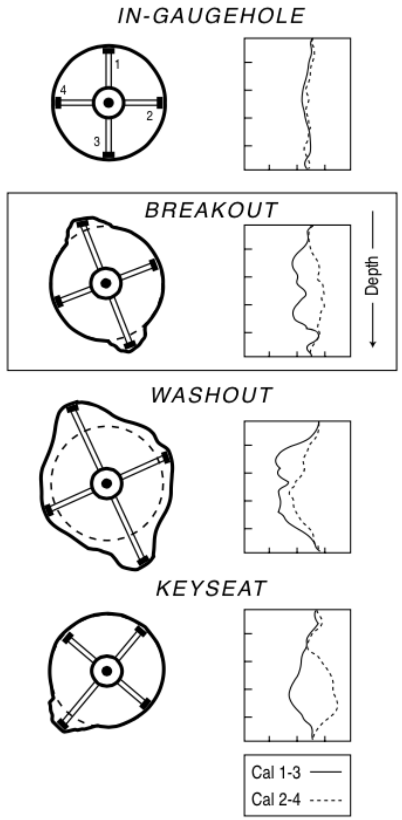
Four-arm caliper data



Caliper data



Breakout indication



Examples of variations

Thermal effects on wellbore stress

Strongly time dependent

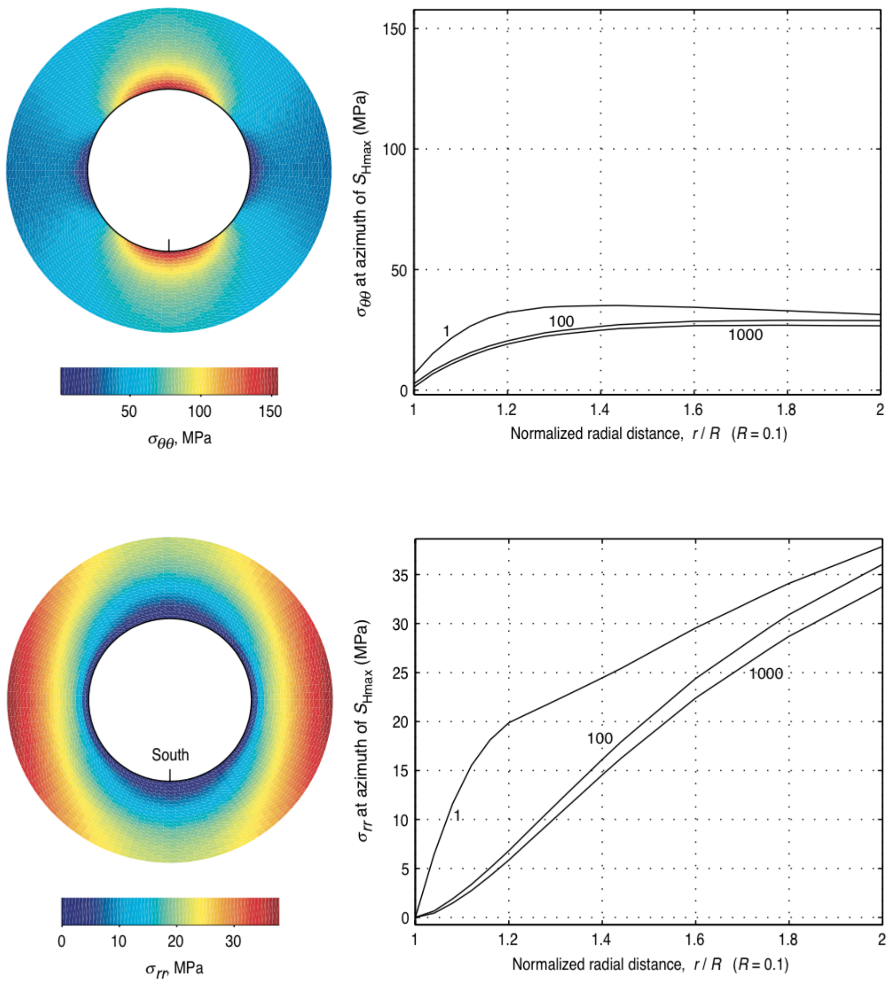
$$\frac{\partial T}{\partial t} = \alpha_T \nabla^2 T$$

$\alpha \rightarrow$ strongly dependenent of the silica content of the rock.

Under steady-state conditions,

$$\Delta\sigma_{\theta\theta}^{T} = \frac{\alpha_T E \Delta T}{1 - \nu}$$

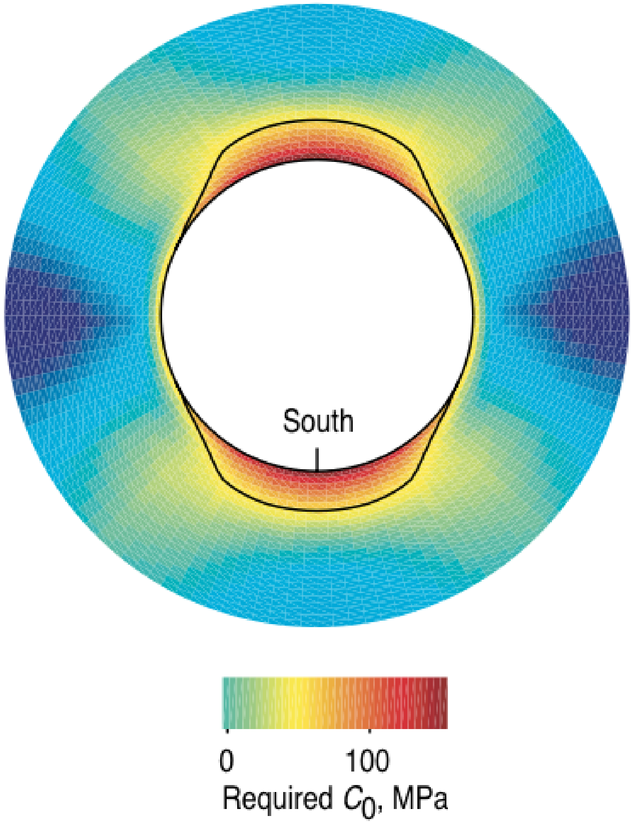
Time-temperature effects



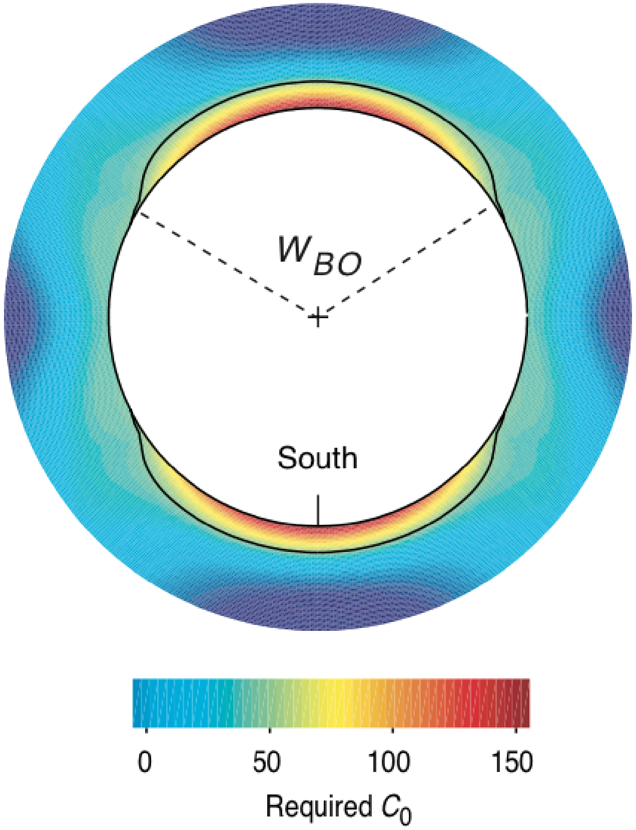
$\Delta T = 25^\circ$ C

$\Delta P = 6$ MPa

Stability through cooling?

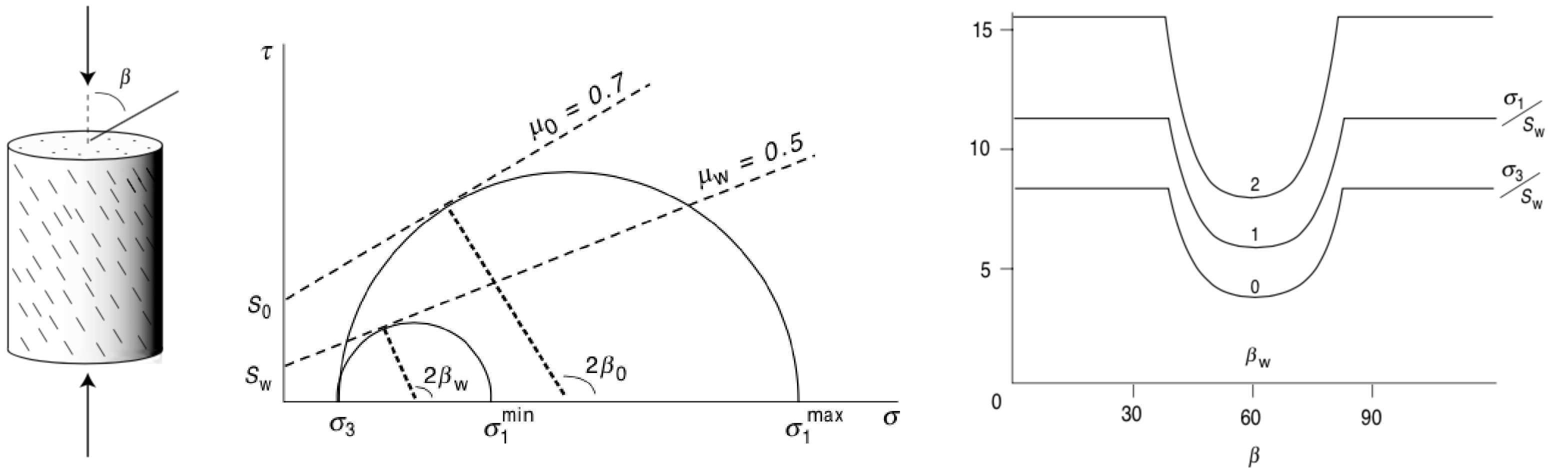


Cooling



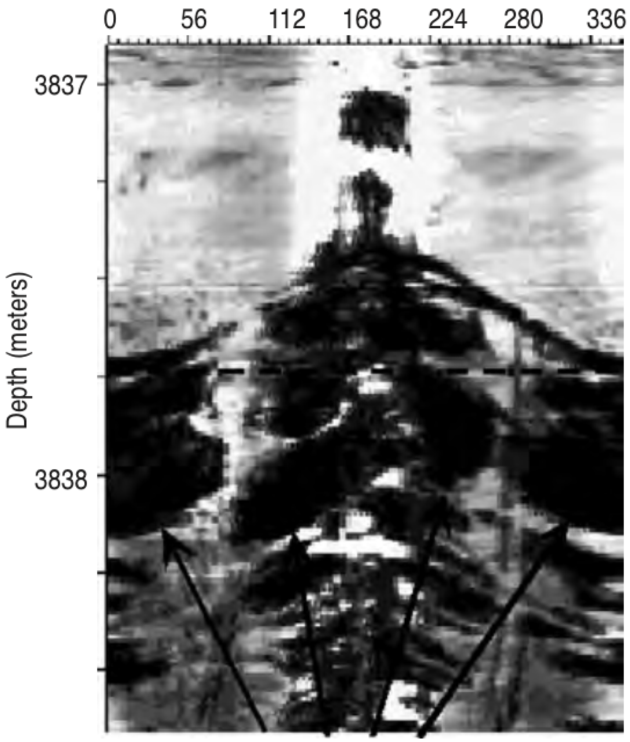
Reference

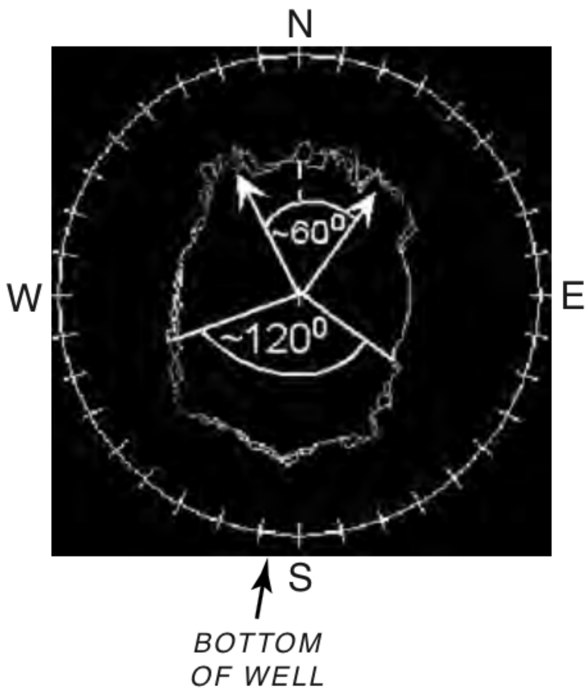
Rock strength anisotropy



$$\sigma_1 = \sigma_3 \frac{2(S_w + \mu_w \sigma_3)}{(1 - \mu_w \cot \beta_w) \sin 2\beta}$$

Rock strength anisotropy effects on breakouts

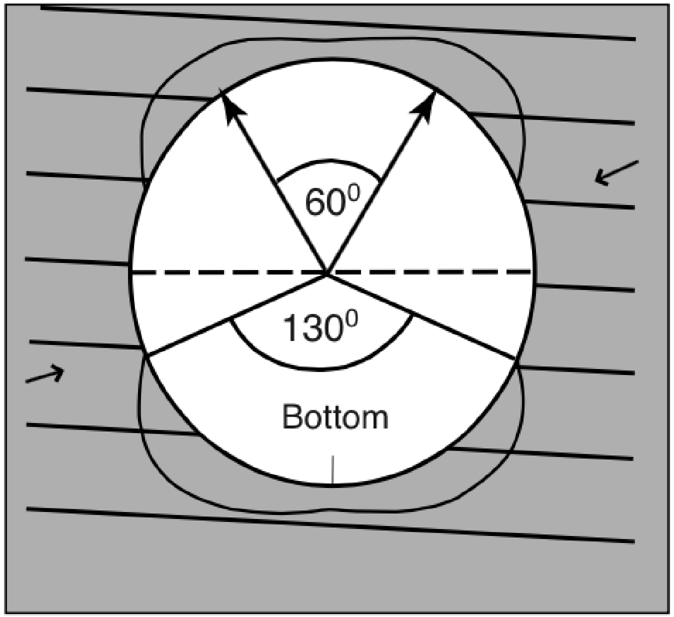




 Zoback, *Reservoir Geomechanics* (Fig. 6.16a,b pp. 199)

Two mechanisms

- Stresses exceed intact rock strength
- Stresses activate slip on weak bedding planes



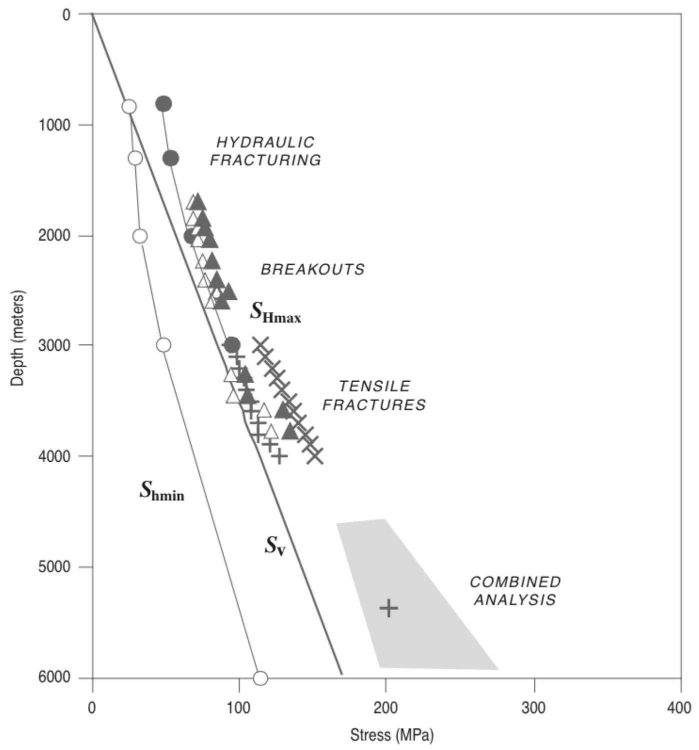
Chemical effects

- Water Activity ($A_w \sim \frac{1}{\text{salinity}}$) can to increased pore pressure

S_{Hmax} from breakout data

$$S_{Hmax} = \frac{(C_0 + 2P_p + \Delta P + \Delta\sigma^T) - S_{hmin}(1 + 2\cos(\pi - w_{bo}))}{1 - 2\cos(\pi - w_{bo})}$$

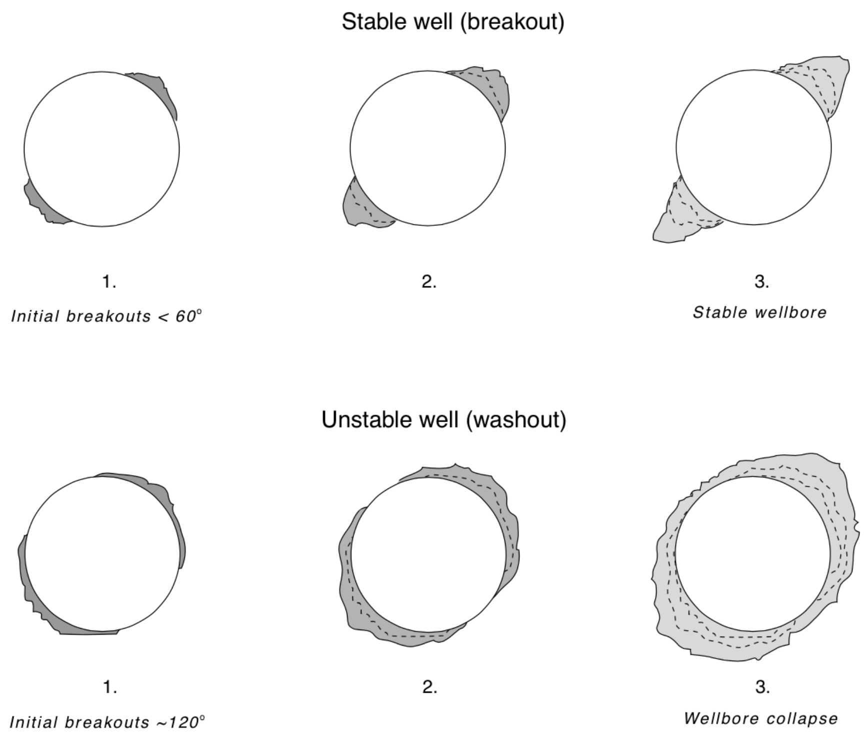
Example



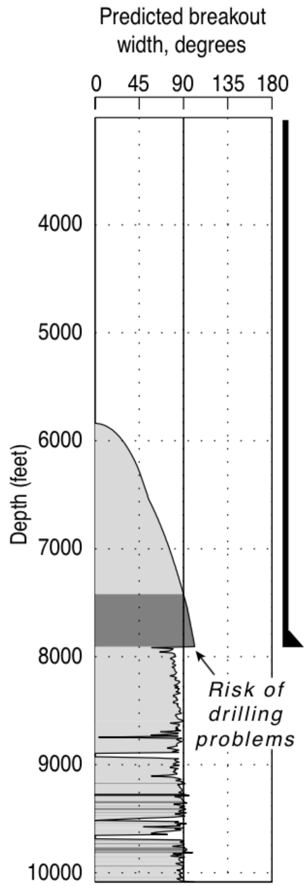
 Zoback, *Reservoir Geomechanics* (Fig. 7.7 pp. 223)

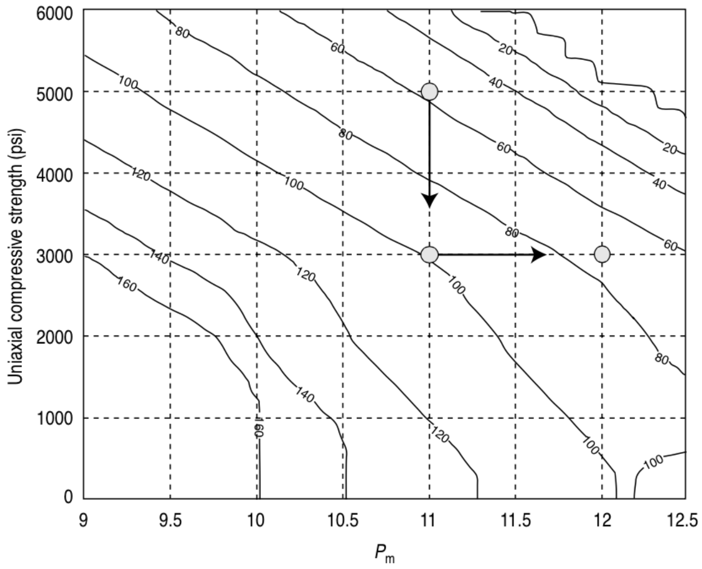
Wellbore stability

Defining a "stable" wellbore



Emperical model: Maximum 90° breakouts





Comprehensive model

i.e. why your studying geomechanics