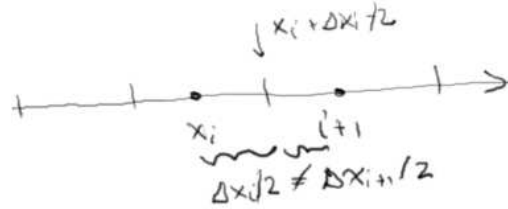


$$\sum_{i=0}^{N-1} \left\{ \underbrace{\frac{V(x) c_t \phi}{B_{\alpha}}}_{B(x)} \frac{\partial p(x,t)}{\partial t} - \frac{1}{B_{\alpha}} \left[A(x) \frac{k(x)}{\mu(x)} \frac{\partial p(x)}{\partial x} \right]_{x_i - \Delta x_i/2}^{x_i + \Delta x_i/2} \right\} = 0$$

$B(x)$
↓
 B_i

$k(x_i + \Delta x_i/2) = k_{i+1/2}$, likewise A, μ
 $k(x_i - \Delta x_i/2) = k_{i-1/2}$

$$\sum_{i=0}^{N-1} \left\{ B_i \frac{\partial p_i}{\partial t} - \frac{1}{B_{\alpha}} \left[\frac{A_{i+1/2} k_{i+1/2}}{\mu_{i+1/2}} \frac{\partial p_{i+1/2}}{\partial x} - \frac{A_{i-1/2} k_{i-1/2}}{\mu_{i-1/2}} \frac{\partial p_{i-1/2}}{\partial x} \right] \right\} = 0$$



$$\sum_{i=0}^{N-1} \left\{ B_i \frac{\partial p_i}{\partial t} - \frac{1}{B_{\alpha}} \left[\frac{A_{i+1/2} k_{i+1/2}}{\mu_{i+1/2}} \frac{(p_{i+1} - p_i)}{\Delta x_{i+1/2}} - \frac{A_{i-1/2} k_{i-1/2}}{\mu_{i-1/2}} \frac{(p_i - p_{i-1})}{\Delta x_{i/2} + \Delta x_{i-1/2}} \right] \right\} = 0$$

$\Delta x_{i+1/2} = \frac{\Delta x_{i+1} + \Delta x_i}{2}$, $\Delta x_{i-1/2} = \frac{\Delta x_i + \Delta x_{i-1}}{2}$

$$\sum_{i=0}^{N-1} \left\{ B_i \frac{\partial p_i}{\partial t} + \left[\frac{A_{i+1/2} k_{i+1/2}}{B_{\alpha} \mu_{i+1/2} \Delta x_{i+1/2}} (p_i - p_{i+1}) + \frac{A_{i-1/2} k_{i-1/2}}{B_{\alpha} \mu_{i-1/2} \Delta x_{i-1/2}} (p_i - p_{i-1}) \right] \right\} = 0$$

$T_{i+1/2} = \frac{A_{i+1/2} k_{i+1/2}}{B_{\alpha} \mu_{i+1/2} \Delta x_{i+1/2}}$

$T_{i-1/2} = \frac{A_{i-1/2} k_{i-1/2}}{B_{\alpha} \mu_{i-1/2} \Delta x_{i-1/2}}$

$$\sum_{i=0}^{N-1} \left\{ B_i \frac{\partial p_i}{\partial t} + \left[T_{i+1/2} (P_i - P_{i+1}) + T_{i-1/2} (P_i - P_{i-1}) \right] \right\} = 0$$

$$B_0 \frac{\partial p_0}{\partial t} + B_1 \frac{\partial p_1}{\partial t} + \dots + B_{N-1} \frac{\partial p_{N-1}}{\partial t} + \left[T_{-1/2} (P_0 - P_{-1}) + T_{1/2} (P_0 - P_1) \right] \\ + \left[T_{1/2} (P_1 - P_0) + T_{3/2} (P_1 - P_2) \right] + \dots + \left[T_{N-3/2} (P_{N-1} - P_{N-2}) + T_{N-1/2} (P_{N-1} - P_N) \right] = 0$$

$$\underbrace{\begin{bmatrix} B_0 & & & \\ & B_1 & & \\ & & \ddots & \\ & & & B_{N-1} \end{bmatrix}}_{[B]} \left\{ \frac{\partial \vec{p}}{\partial t} \right\} + \begin{bmatrix} T_{1/2} + T_{1/2} & -T_{1/2} & 0 & \dots \\ -T_{1/2} & T_{1/2} + T_{3/2} & -T_{3/2} & 0 \\ 0 & -T_{3/2} & T_{3/2} + T_{5/2} & -T_{5/2} \\ \dots & \dots & \dots & T_{N-3/2} + T_{N-1/2} \end{bmatrix} \left\{ \vec{p} \right\} = \left\{ \vec{Q} \right\}$$

$$[B] \left\{ \frac{\partial \vec{p}}{\partial t} \right\} + [T] \left\{ \vec{p} \right\} = \left\{ \vec{Q} \right\} \quad \leftarrow$$