

$$[I]\{\vec{p}^{n+1}\} - [J]\{\vec{p}^n\} + \eta[A]\{\vec{p}\} = \{\vec{p}_s\} \quad \equiv [psi]$$

Multiply on left by $\frac{1}{\Delta t}[B]$

rate form
↓

$$\frac{1}{\Delta t}[B]\{\vec{p}^{n+1}\} - \frac{1}{\Delta t}[B]\{\vec{p}^n\} + \underbrace{\frac{\eta}{\Delta t}[B][A]}_{[T]}\{\vec{p}\} = \underbrace{\frac{1}{\Delta t}[B]\{\vec{p}_s\}}_Q = \left[\frac{ft^3}{day}\right]$$

$$B = \begin{bmatrix} \frac{V_0 \phi C_t}{B_r} & 0 & 0 & 0 & \dots & 0 \\ \vdots & \frac{V_1 \phi C_t}{B_r} & & & \vdots & \\ \vdots & & \frac{V_2 \phi C_t}{B_r} & & & 0 \\ \vdots & & & \dots & \frac{V_{n-1} \phi C_t}{B_r} & \\ 0 & \dots & 0 & \dots & 0 & \dots \end{bmatrix}$$

"Accumulation"

$$V_i = A_i \Delta x$$

$$[T] = \begin{bmatrix} \dots & \dots & \dots & \dots & \dots \\ -T & 2T & -T & 0 & \dots \\ \dots & -T & 2T & -T & \dots \\ \dots & \dots & \dots & \dots & \dots \end{bmatrix}$$

$$T = \frac{k A_i}{\mu B_r \Delta x}$$

"Transmissibility"

evaluate \vec{p} @ \vec{p}^n

$$\{\vec{p}^{n+1}\} = \{\vec{p}^n\} + \Delta t [B]^{-1} (\{\vec{Q}\} - [T]\{\vec{p}^n\})$$

Explicit

evaluate \vec{p} @ \vec{p}^{n+1}

$$\{\vec{p}^{n+1}\} = \left([T] + \frac{1}{\Delta t} [B] \right)^{-1} \left(\frac{1}{\Delta t} [B] \{\vec{p}^n\} + \{\vec{Q}\} \right)$$

Implicit

Transmissibility Form